

# Firms' Strategies and Markets Entry

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# Introduction

- ▶ Entrant's strategy: "Judo economics"
- ▶ Incumbent's strategies vis-à-vis entry
  - ▶ Entry deterred
  - ▶ Entry Accomodated

# Entrant's strategy: Judo Economics

**In the art of "judo", a combatant uses the weight and strenght of his opponent to his own advantage.**

- ▶ *Value-based* judo strategy
- ▶ *Rule-based* judo strategy

1. Softsoap on the liquid soap market
2. Red Bull on the energy drinks market

*Ruled-based* judo strategy

# Softsoap Case

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- A vertical timeline with red dots and lines indicating key events in the Softsoap case. The events are as follows:
- 1970s**: Minnetonka Corporation was facing slowing sales: \$25 million.
  - 1977**: US bar soap industry had sales of \$1.5 billion. Industry dominated by 4 large firms "Armour Dial, P&G, Lever Brothers, Colgate Palmolive".
  - 1980**: Minnetonka created a new product, a liquid soap. Minnetonka launched Softsoap at \$1.49. Spent \$7 million on advertising. Sales of Softsoap reached \$39 million.
  - 1983**: P&G released a liquid soap product under the name "Rejoice". With aggressive strategies, they achieved 30% market share.
  - 1985**: Minnetonka still market leader with Softsoap in a \$100 million market.
  - 1987**: Minnetonka sold Softsoap to Colgate-Palmolive for \$61 million.

Insight: Softsoap had a novel product. Major incumbents could have imitated quickly and use their brand name to dominate the market but they were hesitant (risk of cannibalisation of softsoap+ risk of tarnishing their image).

# Red Bull Case

- 1987 ● | Founded in Austria by Dietrich Mateschitz. Red Bull began with sales to discos where alcohol was prohibited.
- 1997 ● | Sold for a decade before entering the US. market. Carbonated soft drinks largest beverage market in the US (>\$50 billion)  
US energy drinks market were not interesting yet for large players (\$75 million)
- 2001 ● | Rumors of being made of bulls' testicles. 3 swedes died (because of mix with alcohol). Red Bull now looks dangerous. Red Bull had grown its sales 118% over the past year (about 2/3 of the energy drink market), while overall soft drinks grew by only 0.6% (total US energy drink market size: \$275 million)
- 2001 ● | Coke launch its energy drink KMX with a marketing strategy based on secrecy and mystery.

Insight: Soft drinks don't really see it as a new product at first because it is just caffeine. Then Red Bull deliberately aligned with dangerous sporting events. Soft drinks launch their energy drinks on a different brand name to escape this image.

## Judo Economics: Gelman and Salop (1983)

- ▶ Consumers have an inelastic demand of size  $D$  if  $p \leq p_{max}$ .
- ▶ An incumbent  $I$  has an installed capacity  $D$  and no production cost.
- ▶ An entrant  $E$  has a variable cost  $c_E > 0$

The timing of the game is as follows:

1. E decides to enter or not the market. If he enters, he sets a capacity  $K_E$  and its price  $p_E$ .
2. The incumbent observes  $(K_E, p_E)$  and adapts its price denoted  $p_I$ .

**If  $E$  does not enter the market**

- ▶  $E$  gets 0 and  $I$  is a monopolist.
- ▶ A monopolist  $I$  sets a price  $p_{\max}$  and its profit is  $p_{\max}D$ .

If  $E$  chooses to enter the market,

- ▶ If  $p_I > p_E$  the firm  $E$   $D_E = K_E$  and  $D_I = D - K_E$ . Firm  $I$  can sell at  $p_{max}$  and obtain a profit

$$p_{max}(D - K_E)$$

•

- ▶ If  $p_I \leq p_E$ , the firm I has a demand  $D_I = D$  and  $D_E = 0$ . The firm can also sell at  $p_E - \epsilon$  and obtain  $p_E D$ .
- ▶ I chooses the price that maximizes its profit i.e.:  $p_{max}$  if  $p_E \leq \frac{p_{max}(D - K_E)}{D}$  and  $p_E$  otherwise.

- $$K_E \left( \frac{D - K_E}{D} p_{max} - c_E \right)$$

- If  $c_E = 0$ , i.e; the entrant is as efficient as the incumbent,  $K_E^* = \frac{D}{2}$ , the two firms share the market and the price is  $\frac{p_{max}}{2}$ .



$$\Pi_E = \frac{D}{p_{max}} \frac{(p_{max} - c_E)^2}{4}$$

# Strategic Incumbent and entry

1. A taxonomy of incumbent's investments strategies
  - ▶ "Top-dog strategy": investment in capacity
  - ▶ "Lean and hungry look strategy": an innovation model
2. The chain store paradox : a reputation game
3. Exclusive dealing: a contracting strategy

## A taxonomy of incumbent's investments strategies

- ▶ In stage 1, the incumbent chooses the level of some irreversible investment  $K_1$ .
- ▶ In stage 2, after observing  $K_1$ ,  $E$  decides to enter or not. Product market decisions are taken, denoted  $\sigma_1$  and  $\sigma_2$  (price, quantity, investment).
- ▶ If  $E$  enters,  $\sigma_1$  and  $\sigma_2$  are chosen simultaneously, and profits are denoted  $\pi_1(K_1, \sigma_1, \sigma_2)$  and  $\pi_2(K_1, \sigma_1, \sigma_2)$ .

We assume that  $\pi_2(K_1, \sigma_1, \sigma_2)$  includes entry cost if any.

We assume that there exists a unique Nash equilibrium of this competition stage  $(\sigma_1^*(K_1), \sigma_2^*(K_1))$  solution of:

$$\frac{\partial \pi_1(K_1, \sigma_1, \sigma_2)}{\partial \sigma_1} = 0$$

$$\frac{\partial \pi_2(K_1, \sigma_1, \sigma_2)}{\partial \sigma_2} = 0$$

- ▶ If  $E$  does not enter, the incumbent obtains sets  $\sigma_1^m(K_1)$  and obtains  $\pi_1^m(K_1, \sigma_1^m(K_1))$ .

- ▶ Two strategies: Entry deterrence and Accomodation.

## Entry deterrence

- ▶  $K_1$  is set at a level sufficient to deter entry i.e. such that:

$$\pi_2(K_1, \sigma_1^*(K_1), \sigma_2^*(K_1)) = 0$$

- ▶ To see how  $K_1$  must be distorted, we totally differentiate  $\pi_2$  with respect to  $K_1$  :

$$\frac{d\pi_2}{dK_1} = \underbrace{\frac{\partial \pi_2}{\partial K_1}}_{\text{Direct Effect}} + \underbrace{\frac{\partial \pi_2}{\partial \sigma_1} \frac{\partial \sigma_1^*(K_1)}{\partial K_1}}_{\text{Strategic Effect}} + \underbrace{\frac{\partial \pi_2}{\partial \sigma_2} \frac{\partial \sigma_2^*(K_1)}{\partial K_1}}_{0 \text{ Envelop theorem}}$$

- ▶ Sign of direct effects : advertising informative ( $\frac{\partial \pi_2}{\partial K_1} > 0$ ) or persuasive ( $\frac{\partial \pi_2}{\partial K_1} < 0$ ), investment in capacity ( $\frac{\partial \pi_2}{\partial K_1} = 0$ )
- ▶ Strategic effect : given  $K_1$  it is a commitment for the incumbent to be tough or weak in its decision of  $\sigma_1(K_1)$
- ▶ If  $\frac{d\pi_2}{dK_1} < 0$ , investment makes the incumbent tough: "top dog"; If  $\frac{d\pi_2}{dK_1} > 0$ , investment makes the incumbent soft: "lean and hungry look".

## Entry accomodation

- $K_1$  is set at its best accomodating level, i.e. :

$$\max_{K_1} \pi_1(K_1, \sigma_1^*(K_1), \sigma_2^*(K_1))$$

- To see how  $K_1$  must be distorted, we totally differentiate  $\pi_1$  with respect to  $K_1$  :

$$\frac{d\pi_1}{dK_1} = \underbrace{\frac{\partial \pi_1}{\partial K_1}}_{\text{Direct Effect}} + \underbrace{\frac{\partial \pi_1}{\partial \sigma_1} \frac{\partial \sigma_1^*(K_1)}{\partial K_1}}_{0 \text{ Envelop theorem}} + \underbrace{\frac{\partial \pi_1}{\partial \sigma_2} \frac{\partial \sigma_2^*(K_1)}{\partial K_1}}_{\text{Strategic Effect}}$$

- The direct effect is the "profit maximizing effect" with no effect on firm 2.
- The strategic effect:

$$\text{Sign}\left(\frac{\partial \pi_1}{\partial \sigma_2} \frac{\partial \sigma_2^*(K_1)}{\partial K_1}\right) = \text{Sign}\left(\frac{\partial \pi_2}{\partial \sigma_1} \frac{\partial \sigma_1^*(K_1)}{\partial K_1}\right) \times \text{Sign}\left(\frac{d\sigma_2^*}{d\sigma_1}\right)$$



## A top dog example: Investment in capacity

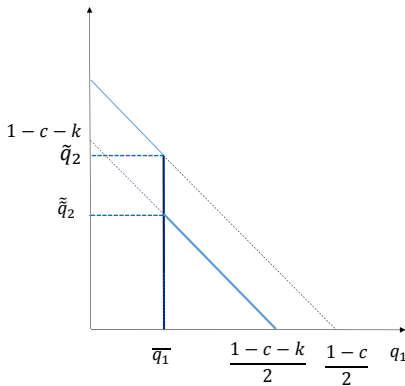
- ▶ In stage 1, an incumbent firm 1 sets its capacity  $\bar{q}_1$ .
- ▶ In stage 2, the entrant 2 decides to enter or not. In case of entry the two firms set additional capacity  $\Delta\bar{q}_1$  and  $\Delta\bar{q}_2$  respectively and produce at most  $\bar{q}_1 + \Delta\bar{q}_1$  for the incumbent and  $\Delta\bar{q}_2$  for the entrant.
- ▶ Products are homogeneous and the inverse demand function is  $P = 1 - q_1 - q_2$ .
- ▶ Entry cost :  $e$
- ▶  $k$  is the marginal cost of capacity.
- ▶  $c$  the marginal cost of production.

Assume that 2 has entered. The incumbent's profit is:

$$\pi_1 = (1 - q_1 - q_2 - c)q_1 - k\Delta\bar{q}_1$$

Maximizing this function with respect to  $q_1$  it follows that the best reaction function is:

$$q_1(q_2) = \begin{cases} \frac{1}{2}(1 - q_2 - c - k) & \text{for } q_1 > \bar{q}_1, \\ \frac{1}{2}(1 - q_2 - c) & \text{for } q_1 \leq \bar{q}_1 \end{cases}$$





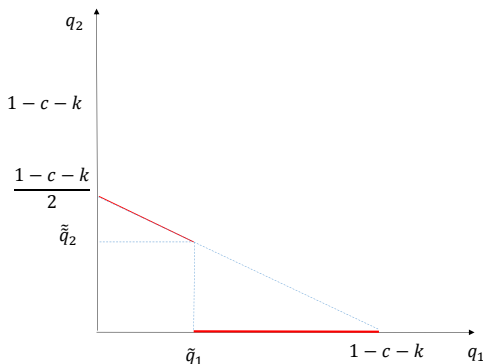
The entrant's profit is:

$$\pi_2 = (1 - q_1 - q_2 - c)q_2 - k\Delta\bar{q}_2 - e$$

Maximizing this function w.r.t.  $q_2$ , the best reaction function is:

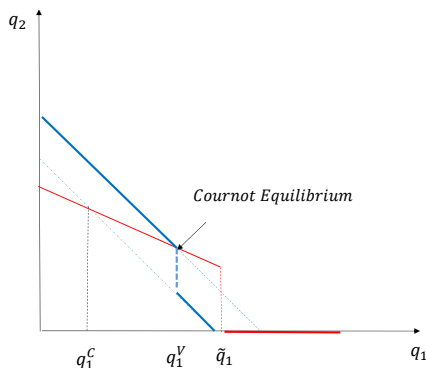
$$q_2(q_1) = \begin{cases} \frac{1}{2}(1 - q_1 - c - k) & \text{for } q_1 < \tilde{q}_1, \\ 0 & \text{for } q_1 \geq \tilde{q}_1 \end{cases}$$

$$\tilde{q}_1 = 1 - c - k - 2\sqrt{e} \Leftrightarrow \pi_2(q_2(q_1), q_1) = \frac{1}{4}(1 - q_1 - c - k)^2 - e = 0$$



## 4 cases to consider

1. Inevitable entry:  $\tilde{q}_1 > q_1^V \Rightarrow e < e^- = \frac{1}{9}(1 - c - 2k)^2$ .  $q_1^V$  corresponds to a Nash equilibrium between the entrant 2 and an unconstrained firm 1.
- ▶ if  $\bar{q}_1 = q_1^V \Rightarrow \pi_1 = \frac{1}{9}(1 - c + k)(1 - c - 2k)$
- ▶ if  $\bar{q}_1 = q_1^C \Rightarrow \pi_1^C = \frac{1}{9}(1 - c - k)^2$ .

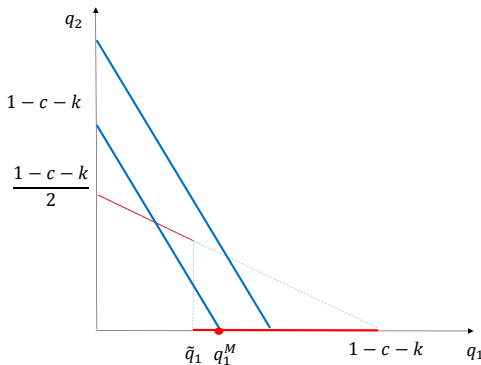


## 4 cases to consider

### 2. Blockaded entry

$$q_1^M = \frac{1}{2}(1 - c - k) \text{ and } q_1^M > \tilde{q}_1 \Rightarrow e > e^+ = \frac{1}{16}(1 - c - k)^2$$

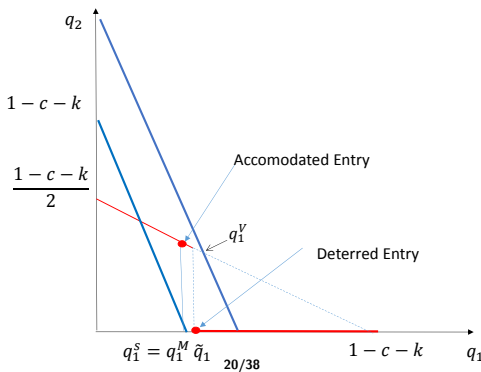
► Then  $\bar{q}_1 = q_1^M \Rightarrow \pi_1^M = \frac{1}{4}(1 - c - k)^2$



## 4 cases to consider

If  $q_1^M < \tilde{q}_1 < q_1^V \Leftrightarrow e^- < e < e^+$

3. Deterred entry  $\bar{q}_1 = \tilde{q}_1$  — Commitment from 1 to be on its highest reaction function  $\Rightarrow$  credible that  $q_1 = \tilde{q}_1$  and no entry.
4. Accommodated entry
  - $\bar{q}_1 = q_1^S = \frac{1}{2}(1 - c - k) = q_1^M < \tilde{q}_1$ . In the competition stage, 1 is on the high reaction function only if  $q_1 < q_1^M < q_1^V$ .



If  $q_1^M < \tilde{q}_1 < q_1^V \Leftrightarrow e^- < e < e^+$

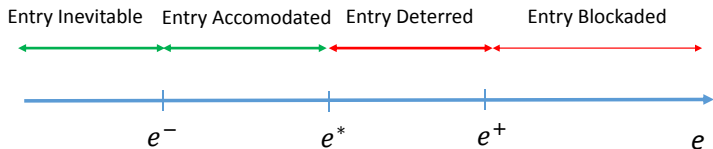
- ▶ The profit obtained in case of accomodation is:

$$\max_{q_1^S} \pi_1(q_1^S, q_2(q_1^S)) = \frac{1}{2}(1 - c - k - q_1^S)q_1^S \Rightarrow \pi_1^A = \frac{1}{8}(1 - c - k)^2$$

- ▶ To deter entry, the incumbent must install a larger capacity  $\tilde{q}_1$  and its profit is:

$$\pi_1^D = (1 - c - k - \tilde{q}_1)\tilde{q}_1 = 2\sqrt{e}(1 - c - k - 2\sqrt{e})$$

It is possible to show that  $\pi_1^D > \pi_1^A$  if  $e > e^* = \frac{(2-\sqrt{2})^2(1-c-k)^2}{64}$ .



## Remember

This investment capacity model illustrates the TOP DOG strategy for Deterrence:

- ▶ Deterrence  $\rightarrow q_1 = \tilde{q}_1$  which corresponds to a capacity expansion above the monopoly level.
- ▶ Accomodation  $\rightarrow q_1^S = q_1^M$  which corresponds to a capacity expansion above the competition level ( $q_1^C = \frac{1-c-k}{3}$ ).

# Lean and Hungry look: An innovation model

## Assumptions

- **Period 1:** Firm 1 can make an investment  $K_1$  to reduce its marginal cost  $c(K_1)$  and obtain the corresponding gross profit  $\pi^M(c(K_1))$  which strictly increases in  $K_1$  in period 1.
- **Period 2** Firm 2 may enter at a fixed cost  $F$ . When firm 2 enters, 1 and 2 compete in  $R\&D$ :
  - To innovate with probability  $\rho_i$  costs  $\rho_i^2/2$ .

Innovation is drastic and leads to a marginal cost  $c$ .

Table: Gains in period2

Innovation probabilities	$\rho_2$	$(1 - \rho_2)$
$\rho_1$	$(0, 0)$	$(\pi^M(c), 0)$
$(1 - \rho_1)$	$(0, \pi^M(c))$	$(\pi^M(c(K_1), 0)$

**Period 2:** Firms 1 and 2 choose their *R&D* levels  $\rho_1$  and  $\rho_2$  to maximize their expected profit:

$$\begin{aligned}\pi_1 &= \rho_1(1 - \rho_2)\pi^M(c) + (1 - \rho_1)(1 - \rho_2)\pi^M(c(K_1)) - \rho_1^2/2, \\ \pi_2 &= \rho_2(1 - \rho_1)\pi^M(c) - \rho_2^2/2\end{aligned}$$

FOCS are:

$$\begin{cases} (1 - \rho_2^*)(\pi^M(c) - \pi^M(c(K_1))) = \rho_1^*, \\ (1 - \rho_1^*)\pi^M(c) = \rho_2^* \end{cases}$$

The equilibrium investments  $\rho_1^*$  and  $\rho_2^*$  that solve the above system are such that  $\frac{\partial \rho_1^*}{\partial K_1} < 0$  and  $\frac{\partial \rho_2^*}{\partial K_1} > 0$ . FOC

**Deterrence**

$$\frac{d\pi_2(K_1, \rho_1^*, \rho_2^*)}{dK_1} = -\rho_2^*\pi^M(c)\frac{\partial \rho_1^*}{\partial K_1} > 0$$

The deterrence strategy consists in reducing  $K_1$ .



## Accommodation

$$\begin{aligned}\frac{d\pi_1(K_1, \rho_1^*, \rho_2^*)}{dK_1} &= \frac{\pi_1(K_1, \rho_1^*, \rho_2^*)}{\partial K_1} - (\rho_1^* \pi^M(c) + (1 - \rho_1^*) \pi^M(c(K_1))) \frac{\partial \rho_2^*}{\partial K_1} \\ &< \frac{\pi_1(K_1, \rho_1^*, \rho_2^*)}{\partial K_1}\end{aligned}$$

where  $\frac{\pi_1(K_1, \rho_1^*, \rho_2^*)}{\partial K_1} = (1 - \rho_1^*)(1 - \rho_2^*) \frac{\partial \pi^M(c(K_1))}{\partial K_1}$

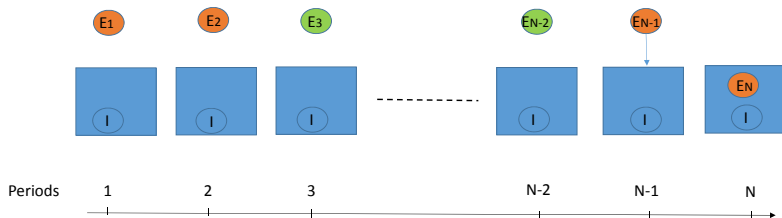
The accommodation strategy consists in reducing  $K_1$ .

## Lean and Hungry look

In period 1 firm 1 underinvests in  $K_1$  to commit itself to being more aggressive in its *R&D* race in period 2. This is the best strategy both to deter entry or accommodate.

**Why?** *R&D* investments are strategic substitutes and the larger  $K_1$  the higher  $\pi^M(c(K_1))$  and therefore the lower the incumbent's incentive to invest in period 2 (Arrow replacement effect).

## The chain store paradox (Selten, 1978)



- ▶ An incumbent firm  $I$  which owns stores in  $N$  markets.
- ▶ Entry takes place sequentially
  1.  $E_1$  enters or not in period 1 on a first market.
  2. Another  $E_2$  enters or not on a second market in period 2.
  3. ...
  4. The last  $E_N$  enters or not on market  $N$  in period  $N$ .

- ▶ Without entry the gain of I in each store is:  $a$
- ▶ In case of entry, gains of firm I and  $E_i$  are:

Table: Payoffs in case of entry

Choice of I	Fight	Accomodate
Payoffs (I, $E_i$ )	$(-1, -1)$	$(0, b)$

- ▶ We solve the game backward.
- ▶ In period  $N$ , if  $E_N$  enters, the best choice for player I is to accomodate. Long run consideration do not come in, since after period  $N$  the game is over.
- ▶ In period  $N - 1$ , a fight in period  $N - 1$  would not deter player  $N$  to enter, therefore in  $N - 1$  the best strategy for I is to accomodate.
- ▶ By induction theory, the unique sequential equilibrium is such that in each period  $t$ ,  $E_t$  enters and I accomodates.
- ▶ Selten Paradox (1978): Incomplete information framework, i.e. I can be of type tough or weak with a probability  $\Rightarrow$  a reputation issue!!

## The chain store game with reputation

- ▶ Same framework except that I can be tough (on all markets) with probability ( $p$ ) and weak with proba ( $1-p$ )
- ▶ Each  $E_i$  can be tough with probability ( $q$ ) and weak with proba ( $1-q$ )
- ▶ **Tough I always fights ; Tough  $E_i$  always enters.**

Table: Payoffs in case of entry

Choice of a weak I	Fight	Accomodate
Payoffs ( $I, E_i$ )	$(-1, -1)$	$(0, b)$

- ▶ We solve the game backward.

## The case $N = 1$

It is a one period game  $\Rightarrow$  **No reputation effect.**

- ▶ **A tough I fights.**
- ▶ A weak I accomodates.
- ▶  $p$  is the probability that the incumbent is tough.
- ▶ When the expected gain of a weak  $E_1$  is  $-p + (1 - p)b > 0$ , i.e.  $p < \underline{p} = \frac{b}{b+1}$ ,  $E_1$  enters. Otherwise,  $E_1$  stays out.
- ▶ If  $p < \underline{p} = \frac{b}{b+1}$ , a weak I gains 0. If  $p \geq \underline{p} = \frac{b}{b+1}$ , I gains  $a$ .

## The case $N = 2$

It is a two-period game  $\Rightarrow$  **A reputation effect may take place.**

- ▶ **A tough I fights.**
- ▶ What is the strategy for a weak I?
  - ▶ If I accommodates in  $t = 1$ , then, in  $t = 2$ ,  $E_2$  knows that I is weak and always enters. The expected gain of a weak I is 0.
  - ▶ If I fights in  $t = 1$ , and if then in  $t = 2$   $E_2$  believes that I is tough and stays out, the expected gain of a weak I is  $-1 + \delta(1 - q)a$  (with the complementary probability  $q$ ,  $E_2$  is **tough and enters**).

If  $-1 + \delta(1 - q)a < 0$ , there is **No reputation strategy** for a weak I.

In  $t = 1$ , a weak  $E_1$  enters if  $p < \underline{p} = \frac{b}{b+1}$  and stays out otherwise.

- ▶ If I is weak, he accommodates in  $t = 1$ , a weak or tough  $E_2$  enters.
- ▶ If I is tough, he fights in  $t = 1$ , a weak  $E_2$  stays out.

If  $-1 + \delta(1 - q)a > 0$ , **A reputation strategy** for a weak I may arise.

A weak I wants to fight in  $t = 1$  with a positive probability  $\beta$  to deter entry in  $t = 2$ . We focus directly on the interesting case in which  $E_2$  is a weak entrant.

- ▶ If  $p > \underline{p}$ ,
  - ▶ If I accommodates in  $t = 1$ , a weak  $E_2$  knows that I is weak and always enters. Accommodating in  $t = 1$  brings 0 to I.
  - ▶ If I fights in  $t = 1$ , the revised probability that I is tough is  $p(\text{tough}/\text{fight}) = \frac{p}{p + \beta(1-p)} > p > \underline{p}$  and a weak  $E_2$  stays out. Bayes
  - ▶ Because fighting in  $t = 1$  always deters entry in  $t = 2$ , a weak I always fights ( $\beta = 1$ ) in  $t = 1$  and earns the expected profit :  $-1 + \delta(1 - q)a > 0$

If  $-1 + \delta(1 - q)a > 0$ , a weak  $I$  wants to fight in  $t = 1$  with a positive probability  $\beta$  to deter entry in  $t = 2$ .

► If  $p < \underline{p}$ ,

► If  $I$  fights in  $t = 1$ ,  $E_2$  then revises its beliefs accordingly and now believes that  $I$  is tough with a probability:

$$p(\text{tough}/\text{fight}) = \frac{p}{p + \beta(1-p)} > p.$$

► In  $t = 2$ , still  $E_2$  knows that a weak  $I$  accommodates and a tough  $I$  fights (last period) but he takes into account the revised probability that  $I$  is tough  $p(\text{tough}/\text{fight})$ . A weak  $E_2$  is indifferent between entering or not if:

$$-\frac{p}{p + \beta(1-p)} + (1 - \frac{p}{p + \beta(1-p)})b = 0, \text{ i.e. if } \beta^* = \frac{p}{(1-p)b}.$$

► Going backward to  $t = 1$ ,  $E_1$  knows that  $I$  plays this reputation effect to deter entry in  $t = 2$  and therefore anticipates that  $I$  fights with a probability  $p + (1 - p)\beta^* = p\frac{(1+b)}{b}$ .

► A weak  $E_1$  prefers to stay out if  $-p\frac{(1+b)}{b} + (1 - p\frac{(1+b)}{b})b < 0$ , i.e. if  $p > (\frac{b}{1+b})^2$  and  $I$  gains  $a$ . Otherwise if  $p < (\frac{b}{1+b})^2$ , a weak  $E_1$  enters and  $I$  thus gains  $\beta^*(-1 + \delta(1 - q)a) > 0$ .

A lower  $\beta$  would reduce  $I$ 's gains and a higher  $\beta$  cannot block entry of  $E_2$ .



## Conclusion

Because there are at least two-periods,  $E_1$  anticipates that I has an incentive to create a reputation of being tough in  $t = 1$  to deter entry in  $t = 2$ , and therefore  $E_1$  is less likely to enter also in  $t = 1$ .

## The generalization to any $N$ is possible

- Assuming that  $N = 3$ , we now find that  $E_1$  enters if and only if  $p < \left(\frac{b}{1+b}\right)^3$  and so on for  $N = T$  for  $p < \left(\frac{b}{1+b}\right)^T$ .

## Contracts to deter entry

Vertical contracts between manufacturers and retailers might be used to deter entry.

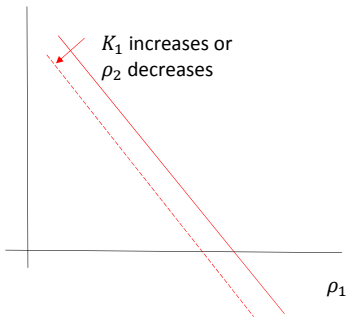
- ▶ For instance bundling or full line forcing practices (Coca-Cola case in Multiproduct pricing class)
- ▶ Exclusive dealing contracts: Mars vs HB case.
  - ▶ The case starts in Ireland in 1989. Ice-cream bars are mostly sold in gas stations.
  - ▶ HB (Unilever) has 79% of the ice-cream bar market and, in 1989, Mars enters.
  - ▶ HB freely supplies small retailers with freezers. Mars market share rises up to 42%.
  - ▶ HB requires exclusivity: only HB ice cream bars are stock in my freezers. Mars's market share decreases to 20%. Mars cannot fight back by offering its own freezers because shops are too small.
  - ▶ The European Court of Justice confirms the EC's prohibition of free freezers in 2003.

## References

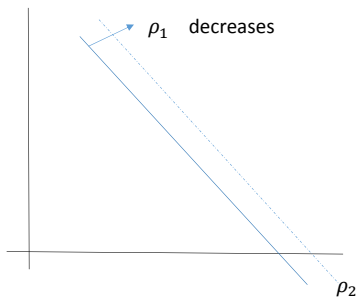
- ▶ Fudenberg, D. and J. Tirole (1991), "Game Theory", MIT Press, Chapter 9.
- ▶ Gelman, J. and S. Salop (1983), "Judo Economics: Capacity Limitation and Coupon Competition", *The Bell Journal of Economics*, 14, 2, p315-325.
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$$\text{FOC } f(\rho_1, \rho_2, K_1) = 0$$
$$f_{\rho_1} < 0$$



$$\text{FOC } g(\rho_1, \rho_2, K_1) = 0$$
$$g_{\rho_2} < 0$$



back

Two events  $A$  and  $B$  respectively occur with probability  $p(A)$  and  $p(B)$ .  
Bayes's rule is as follows:

$$p(A/B) = \frac{p(B/A)P(A)}{p(B)}$$

where conditional probabilities:

- ▶  $p(A/B)$  is the likelihood of event  $A$  occurring given that  $B$  is true;
- ▶  $p(B/A)$  is the likelihood of event  $B$  occurring given that  $A$  is true.

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